

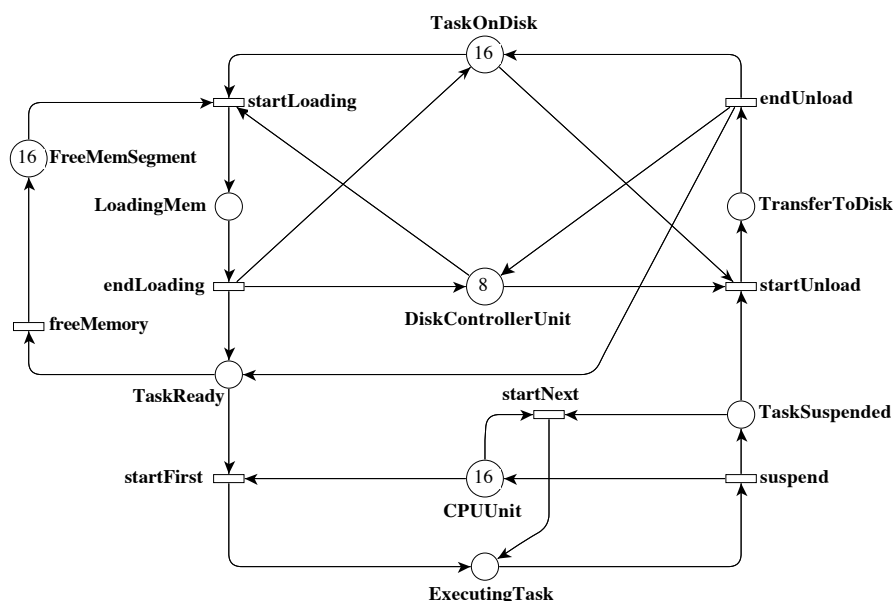
*This form is a summary description of the model entitled "SmallOperatingSystem" proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.*

## Description

This Petri net models a simplified Operating System handling the execution of tasks on a machine with several so-called "memory segments", Disk controller units, and cores. The typical lifecycle of a task is the following:

- 1 A task is loaded from disk to memory (requires a segment and a disk controller),
- 2 When the task is ready to execute, it can get a core, be suspended and get a core again as long as its execution is not finished. It can also be removed from the memory if some is needed otherwise
- 3 When the execution finishes, the task is saved back on the disk.

The system has several scaling parameters:  $M$  (memory segments),  $T$  (tasks),  $D$  (Disk controllers) and  $C$  (cores). However, to simplify this in the MCC, we reduce it to two parameters,  $MT$  and  $DC$  with the following correspondence:  $M = T = MT$ ,  $D = DC$  and  $C = 2 \times DC$ .



Graphical representation for  $MT=16$  and  $DC = 8$

## Scaling parameter

Parameter name	Parameter description	Chosen parameter values
<i>MT</i> and <i>DC</i>	<i>MT</i> to compute available tasks and memory and <i>DC</i> to compute available disk controllers and cores	(MT=16, DC=8), (MT=32, DC=8), (MT=32, DC=16), (MT=64, DC=16), (MT=64, DC=32), (MT=128, DC=32), (MT=128, DC=64), (MT=256, DC=64), (MT=256, DC=128), (MT=512, DC=128), (MT=512, DC=256), (MT=1024, DC=256), (MT=1024, DC=512), (MT=2048, DC=512), (MT=2048, DC=1024), (MT=4096, DC=1024), (MT=4096, DC=2048), (MT=8192, DC=2048), (MT=8192, DC=4096)

## Size of the model

Although the model is parameterized, its size does not depend on parameter values.

number of places: 9  
 number of transitions: 8  
 number of arcs: 27

## Structural properties

<b>ordinary</b> — all arcs have multiplicity one .....	✓
<b>simple free choice</b> — all transitions sharing a common input place have no other input place .....	✗ (a)
<b>extended free choice</b> — all transitions sharing a common input place have the same input places .....	✗ (b)
<b>state machine</b> — every transition has exactly one input place and exactly one output place .....	✗ (c)
<b>marked graph</b> — every place has exactly one input transition and exactly one output transition .....	✗ (d)
<b>connected</b> — there is an undirected path between every two nodes (places or transitions) .....	✓ (e)
<b>strongly connected</b> — there is a directed path between every two nodes (places or transitions) .....	✓ (f)
<b>source place(s)</b> — one or more places have no input transitions .....	✗ (g)
<b>sink place(s)</b> — one or more places have no output transitions .....	✗ (h)
<b>source transition(s)</b> — one or more transitions have no input places .....	✗ (i)
<b>sink transitions(s)</b> — one or more transitions have no output places .....	✗ (j)
<b>loop-free</b> — no transition has an input place that is also an output place .....	✓ (k)
<b>conservative</b> — for each transition, the number of input arcs equals the number of output arcs .....	✗ (l)
<b>subconservative</b> — for each transition, the number of input arcs equals or exceeds the number of output arcs .....	✗ (m)
<b>nested units</b> — places are structured into hierarchically nested sequential units <sup>(n)</sup> .....	✗

(a) 9 arcs are not simple free choice, e.g., the arc from place “TaskOnDisk” (which has 2 outgoing transitions) to transition “startLoading” (which has 3 input places).

(b) transitions “startLoading” and “startUnload” share a common input place “TaskOnDisk”, but only the former transition has input place “FreeMemSegment”.

(c) 7 transitions are not of a state machine, e.g., transition “startLoading”.

(d) 6 places are not of a marked graph, e.g., place “TaskOnDisk”.

(e) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(f) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(g) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(h) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(i) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(j) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(k) stated by CÆSAR.BDD version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

(l) 7 transitions are not conservative, e.g., transition “startLoading”.

(m) 3 transitions are not subconservative, e.g., transition “endLoading”.

(n) the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>

## Behavioural properties

- safe** — *in every reachable marking, there is no more than one token on a place* ..... ✗<sup>(o)</sup>  
**deadlock** — *there exists a reachable marking from which no transition can be fired* ..... ✗  
**reversible** — *from every reachable marking, there is a transition path going back to the initial marking* ..... ✓  
**quasi-live** — *for every transition  $t$ , there exists a reachable marking in which  $t$  can fire* ..... ✓<sup>(p)</sup>  
**live** — *for every transition  $t$ , from every reachable marking, one can reach a marking in which  $t$  can fire* ..... ✓

## Size of the marking graphs

Parameter	Number of reachable markings	Number of transition firings	Max. number of tokens per place	Max. number of tokens per marking
MT=16, DC=8	16 587 <sup>(q)</sup>	100 896 <sup>(r)</sup>	?	≥ 56 <sup>(s)</sup>
MT=32, DC=8	166 515 <sup>(t)</sup>	1 112 454 <sup>(u)</sup>	?	≥ 88 <sup>(v)</sup>
MT=32, DC=16	354 501 <sup>(w)</sup>	2 451 264 <sup>(x)</sup>	?	≥ 112 <sup>(y)</sup>
MT=64, DC=16	7 245 654 <sup>(z)</sup>	29 675 132 <sup>(aa)</sup>	?	≥ 176 <sup>(ab)</sup>
MT=64, DC=32	9 133 641 <sup>(ac)</sup>	67 762 816 <sup>(ad)</sup>	?	≥ 224 <sup>(ae)</sup>
MT=128, DC=32	?	?	?	≥ 352 <sup>(af)</sup>
MT=128, DC=64	?	?	?	≥ 448 <sup>(ag)</sup>
MT=256, DC=64	?	?	?	≥ 704 <sup>(ah)</sup>
MT=256, DC=128	?	?	?	≥ 896 <sup>(ai)</sup>
MT=512, DC=128	?	?	?	≥ 1408 <sup>(aj)</sup>
MT=512, DC=256	?	?	?	≥ 1792 <sup>(ak)</sup>
MT=1024, DC=256	?	?	?	≥ 2816 <sup>(al)</sup>
MT=1024, DC=512	?	?	?	≥ 3584 <sup>(am)</sup>
MT=2048, DC=512	?	?	?	≥ 5632 <sup>(an)</sup>
MT=2048, DC=1024	?	?	?	≥ 7168 <sup>(ao)</sup>
MT=4096, DC=1024	?	?	?	≥ 11264 <sup>(ap)</sup>
MT=4096, DC=2048	?	?	?	≥ 14336 <sup>(aq)</sup>
MT=8192, DC=2048	?	?	?	≥ 22528 <sup>(ar)</sup>
MT=8192, DC=4096	?	?	?	≥ 28672 <sup>(as)</sup>

<sup>(o)</sup> by construction of the model (the initial marking is not safe); confirmed by [CÆSAR.BDD](#) version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

<sup>(p)</sup> stated by [CÆSAR.BDD](#) version 2.6 on all 19 instances ((MT=16, DC=8), (MT=32, DC=8), etc.).

<sup>(q)</sup> computed by PROD in March 2015.

<sup>(r)</sup> computed by PROD in March 2015.

<sup>(s)</sup> lower bound given by the number of initial tokens.

<sup>(t)</sup> computed by PROD in March 2015.

<sup>(u)</sup> computed by PROD in March 2015.

<sup>(v)</sup> lower bound given by the number of initial tokens.

<sup>(w)</sup> computed by PROD in March 2015.

<sup>(x)</sup> computed by PROD in March 2015.

<sup>(y)</sup> lower bound given by the number of initial tokens.

<sup>(z)</sup> computed by PROD in March 2015.

<sup>(aa)</sup> computed by PROD in March 2015.

<sup>(ab)</sup> lower bound given by the number of initial tokens.

<sup>(ac)</sup> computed by PROD in March 2015.

<sup>(ad)</sup> computed by PROD in March 2015.

<sup>(ae)</sup> lower bound given by the number of initial tokens.

<sup>(af)</sup> lower bound given by the number of initial tokens.

<sup>(ag)</sup> lower bound given by the number of initial tokens.

<sup>(ah)</sup> lower bound given by the number of initial tokens.

<sup>(ai)</sup> lower bound given by the number of initial tokens.

<sup>(aj)</sup> lower bound given by the number of initial tokens.

<sup>(ak)</sup> lower bound given by the number of initial tokens.

<sup>(al)</sup> lower bound given by the number of initial tokens.

<sup>(am)</sup> lower bound given by the number of initial tokens.

<sup>(an)</sup> lower bound given by the number of initial tokens.

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<sup>(ao)</sup> lower bound given by the number of initial tokens.  
<sup>(ap)</sup> lower bound given by the number of initial tokens.  
<sup>(aq)</sup> lower bound given by the number of initial tokens.  
<sup>(ar)</sup> lower bound given by the number of initial tokens.  
<sup>(as)</sup> lower bound given by the number of initial tokens.