

This form is a summary description of the model entitled “RefineWMG” proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

Description

Weighted Marked Graphs (WMGs for short) form a well-known and useful subclass of weighted Petri nets in which each place has at most one input and one output. They can model Synchronous Dataflow Graphs [1] (SDFGs), which have been used to model various applications [2,3], notably for designing embedded systems such as Digital Signal Processing (DSPs) applications. These graphs benefit from efficient methods checking their structure and behavior [4,5,6].

However, in general, behavioral properties that are fundamental for many real-world applications, such as liveness and boundedness, remain hard to check in larger classes of Petri nets. So as to alleviate this difficulty, they are often analyzed together with their structural version, namely structural liveness and structural boundedness, which designate respectively the existence of a live marking and the boundedness for every marking. Taken together, structural liveness and structural boundedness define well-formedness. In the sequel, we focus on well-formed nets.

The homogeneous asymmetric-choice (HAC) nets form a subclass of weighted Petri nets in which each pair p, p' of input places of any synchronization satisfies the following: all the outputs of p are also outputs of p' , or conversely; moreover, the homogeneity constraint specifies that for each place p , all the output weights of p are equal. This class generalizes the WMGs and benefits from several structural and behavioral results [7,8,9,10]: some polynomial-time sufficient conditions ensure liveness and boundedness together with their monotonicity, meaning their preservation upon any increase of the marking considered. Such results often rely on decompositions into well-formed join-free components, i.e. well-formed Petri subnets without synchronizations.

The aim is to define first the underlying WMG structure of the system, whose properties are pretty well understood, and then to specify the behavior of each process as a module. Figure 1 pictures such a model, refining some processes of a WMG by merging the corresponding transitions with well-formed, unit-weighted, HAC nets. The marking provided is monotonically live and bounded for each $n \geq 1$.

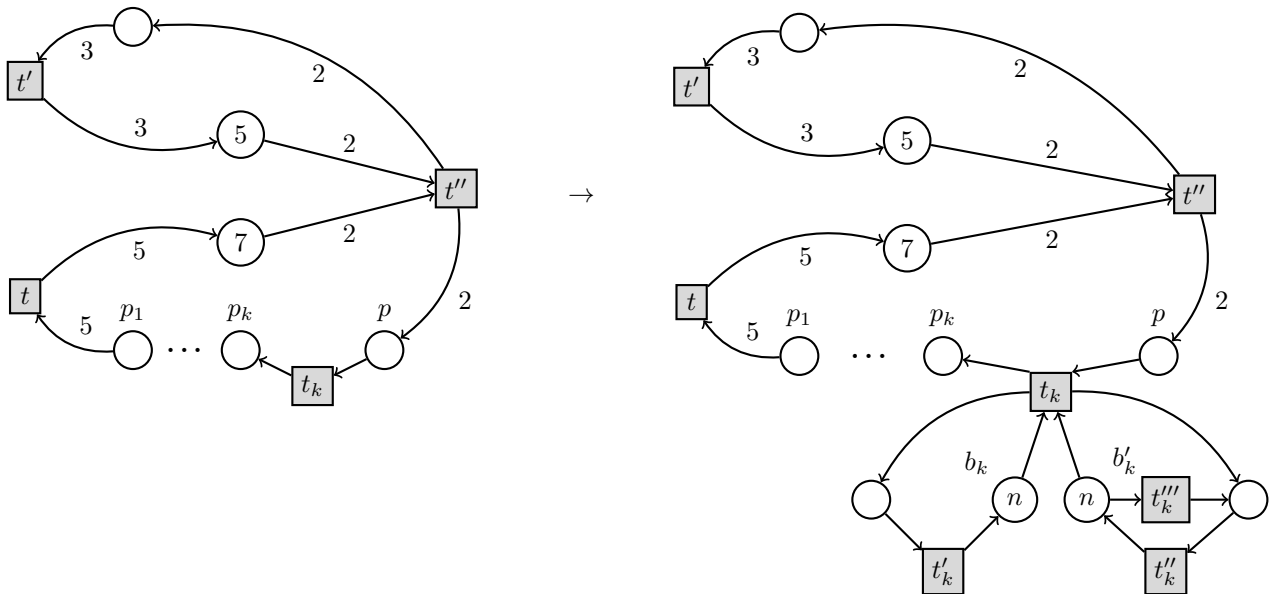


Figure 1: The system on the left is a non-refined WMG with $k \geq 1$ transitions and places on the path $p, t_k, p_k, \dots, p_1, p$ from p to t . On the right, a refinement of the WMG on the left is obtained by merging each transition t_i on this path, $i \in \{1, \dots, k\}$, with a transition of the i -th copy N_i of a unit-weighted HAC system. Two buffers (places) b_i and b'_i of N_i contain n tokens each. The HAC system obtained is live and bounded for each $n \geq 1$.

The model is based on two parameters k and n :

- k denotes the number of HAC modules,
- n is the initial number of tokens in each buffer $b_1, b'_1, \dots, b_k, b'_k$.

References

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Scaling parameter

| Parameter name | Parameter description | Chosen parameter values |
|----------------|---|--|
| k, n | k , the number of modules, and n , the number of initial tokens in each buffer b_i, b'_i in the module N_i for each $i \in \{1, \dots, k\}$. | (2, 2), (2, 3), (5, 5), (5, 6), (7, 7), (7, 8), (10, 10), (10, 11), (15, 15), (15, 16), (25, 25), (25, 26), (50, 50), (50, 51), (100, 100), (100, 101) |

Size of the model

| Parameter | Number of places | Number of transitions | Number of arcs |
|-----------|------------------|-----------------------|----------------|
| $k = 2$ | 14 | 11 | 32 |
| $k = 5$ | 29 | 23 | 68 |
| $k = 7$ | 39 | 31 | 92 |
| $k = 10$ | 54 | 43 | 126 |
| $k = 15$ | 79 | 63 | 186 |
| $k = 25$ | 129 | 103 | 304 |
| $k = 50$ | 254 | 203 | 598 |
| $k = 100$ | 504 | 403 | 1 208 |

Structural properties

- ordinary** — all arcs have multiplicity one X
- simple free choice** — all transitions sharing a common input place have no other input place X

- extended free choice** — *all transitions sharing a common input place have the same input places* X
- state machine** — *every transition has exactly one input place and exactly one output place* X
- marked graph** — *every place has exactly one input transition and exactly one output transition* X
- connected** — *there is an undirected path between every two nodes (places or transitions)* ✓
- strongly connected** — *there is a directed path between every two nodes (places or transitions)* ✓
- source place(s)** — *one or more places have no input transitions* X
- sink place(s)** — *one or more places have no output transitions* X
- source transition(s)** — *one or more transitions have no input places* X
- sink transitions(s)** — *one or more transitions have no output places* X
- loop-free** — *no transition has an input place that is also an output place* ✓
- conservative** — *for each transition, the number of input arcs equals the number of output arcs* ✓
- subconservative** — *for each transition, the number of input arcs equals or exceeds the number of output arcs* ✓
- nested units** — *places are structured into hierarchically nested sequential units^(a)* X

Behavioural properties

- safe** — *in every reachable marking, there is no more than one token on a place* X
- deadlock** — *there exists a reachable marking from which no transition can be fired* X
- reversible** — *from every reachable marking, there is a transition path going back to the initial marking* ✓
- quasi-live** — *for every transition t , there exists a reachable marking in which t can fire* ✓
- live** — *for every transition t , from every reachable marking, one can reach a marking in which t can fire* ✓

Size of the marking graphs

| Parameter | Number of reachable markings | Number of transition firings | Max. number of tokens per place | Max. number of tokens per marking |
|------------|------------------------------|------------------------------|---------------------------------|-----------------------------------|
| $k=2, n=2$ | 58320 | 321732 | ≤ 7 | 20 |
| $k=5, n=5$ | ? | ? | ≤ 7 | 62 |

Other properties

P- and T- semiflows exist and cover the net. The system is live, bounded and reversible for each $n \geq 1$.

^(a)the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>