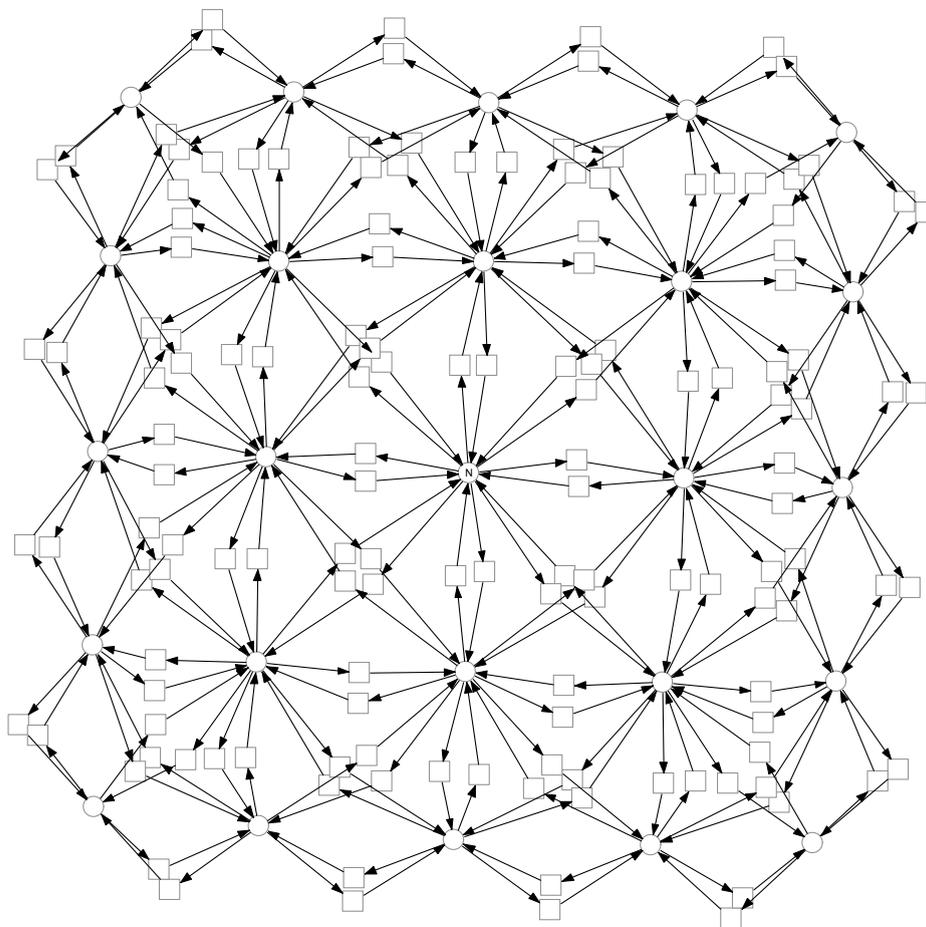


This form is a summary description of the model entitled “Diffusion2D” proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

Description

Diffusion in space is a basic process underlying many spatial (bio-) chemical processes, however typically considered either in the stochastic or continuous setting. The Petri net given here comes from [GHLS13], where it has been used to illustrate the generic modelling of space by use of coloured Petri nets. We discretise the space by a $D \times D$ rectangular grid, D being a model parameter, and deploy the 8-neighbourhood relation with reflecting boundary condition. The process starts with N tokens in the centre position. This model is easily scalable with well-known size of the model growth and its state space.



Graphical representation for $D = 5$, generated by unfolding and automatic layout of a coloured Petri net using Snoopy. There are N tokens in the centre position. All node names are set to invisible.

References

GHLS13 D. Gilbert, M. Heiner, F. Liu and N. Saunders: Colouring Space - A Coloured Framework for Spatial Modelling in Systems Biology; In Proc. PETRI NETS 2013, Milano, Springer, LNCS, volume 7927, pages 230–249, June 2013.

Scaling parameter

Parameter name	Parameter description	Chosen parameter values
D, N	grid size; i.e. there are $D \times D$ grid positions, and initially N tokens in the centre position.	$\langle D = 5, N = 10 \rangle$, $\langle D = 5, N = 50 \rangle$, $\langle D = 5, N = 100 \rangle$, $\langle D = 5, N = 150 \rangle$, $\langle D = 5, N = 200 \rangle$, $\langle D = 5, N = 250 \rangle$, $\langle D = 5, N = 300 \rangle$, $\langle D = 5, N = 350 \rangle$, $\langle D = 10, N = 10 \rangle$, $\langle D = 10, N = 50 \rangle$, $\langle D = 10, N = 100 \rangle$, $\langle D = 10, N = 150 \rangle$, $\langle D = 10, N = 200 \rangle$, $\langle D = 20, N = 10 \rangle$, $\langle D = 20, N = 50 \rangle$, $\langle D = 20, N = 100 \rangle$, $\langle D = 20, N = 150 \rangle$, $\langle D = 30, N = 10 \rangle$, $\langle D = 30, N = 50 \rangle$, $\langle D = 30, N = 100 \rangle$, $\langle D = 30, N = 150 \rangle$, $\langle D = 40, N = 10 \rangle$, $\langle D = 40, N = 50 \rangle$, $\langle D = 40, N = 100 \rangle$, $\langle D = 40, N = 150 \rangle$, $\langle D = 50, N = 10 \rangle$, $\langle D = 50, N = 50 \rangle$, $\langle D = 50, N = 100 \rangle$, $\langle D = 50, N = 150 \rangle$

Size of the model

Parameter	Number of places	Number of transitions	Number of arcs
D	D^2	$8D^2 - 12D + 4$	$2 \cdot T $
$\langle D = 5, N = \dots \rangle$	25	144	288
$\langle D = 10, N = \dots \rangle$	100	684	1368
$\langle D = 20, N = \dots \rangle$	400	2964	5928
$\langle D = 30, N = \dots \rangle$	900	6844	13688
$\langle D = 40, N = \dots \rangle$	1600	12324	24648
$\langle D = 50, N = \dots \rangle$	2500	19404	38808

Structural properties

ordinary — all arcs have multiplicity one	yes
simple free choice — all transitions sharing a common input place have no other input place	yes ^(a)
extended free choice — all transitions sharing a common input place have the same input places	yes ^(b)
state machine — every transition has exactly one input place and exactly one output place	yes ^(c)
marked graph — every place has exactly one input transition and exactly one output transition	no ^(d)
connected — there is an undirected path between every two nodes (places or transitions)	yes ^(e)
strongly connected — there is a directed path between every two nodes (places or transitions)	yes ^(f)
source place(s) — one or more places have no input transitions	no ^(g)
sink place(s) — one or more places have no output transitions	no ^(h)
source transition(s) — one or more transitions have no input places	no ⁽ⁱ⁾
sink transition(s) — one or more transitions have no output places	no ^(j)
loop-free — no transition has an input place that is also an output place	yes ^(k)
conservative — for each transition, the number of input arcs equals the number of output arcs	yes ^(l)

^(a) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(b) stated by [CÆSAR.BDD](#) version 2.6 on all 29 instances (see all aforementioned scaling parameter values).

^(c) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(d) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(e) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(f) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(g) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(h) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

⁽ⁱ⁾ stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(j) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(k) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(l) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

subconservative — for each transition, the number of input arcs equals or exceeds the number of output arcs yes ^(m)
nested units — places are structured into hierarchically nested sequential units ⁽ⁿ⁾ no

Behavioural properties

safe — in every reachable marking, there is no more than one token on a place no ^(o)
dead place(s) — one or more places have no token in any reachable marking ? ^(p)
dead transition(s) — one or more transitions cannot fire from any reachable marking no ^(q)
deadlock — there exists a reachable marking from which no transition can be fired no
reversible — from every reachable marking, there is a transition path going back to the initial marking yes
live — for every transition t , from every reachable marking, one can reach a marking in which t can fire yes

Size of the marking graphs

Parameter	Number of reachable markings	Number of transition firings	Max. number of tokens per place	Max. number of tokens per marking
D, N	$\frac{(D^2+N-1)!}{(D^2-1)! \cdot N!}$?	N	N ^(r)
5, 10	1.3113E+8 ^(s)	5.5537E+9 ^(t)	10 ^(u)	10 ^(v)
5, 50	1.7530E+19 ^(w)	1.7056E+21 ^(x)	50 ^(y)	50 ^(z)
5, 100	2.6011E+25 ^(aa)	3.0206E+27 ^(ab)	100 ^(ac)	100 ^(ad)
5, 150	1.8126E+29 ^(ae)	2.2501E+31 ^(af)	150 ^(ag)	150 ^(ah)
5, 200	1.1439E+32 ^(ai)	1.4707E+34 ^(aj)	200 ^(ak)	200 ^(al)
5, 250	1.8314E+34 ^(am)	2.4062E+36 ^(an)	250 ^(ao)	250 ^(ap)
5, 300	1.2054E+36 ^(aq)	1.6072E+38 ^(ar)	300 ^(as)	300 ^(at)
5, 350	4.2539E+37 ^(au)	?	350 ^(av)	350 ^(aw)
10, 10	4.2634E+13 ^(ax)	2.6754E+15 ^(ay)	10 ^(az)	10 ^(ba)
10, 50	1.3419E+40 ^(bb)	3.0801E+42 ^(bc)	50 ^(bd)	50 ^(be)
10, 100	4.5274E+58 ^(bf)	1.5562E+61 ^(bg)	100 ^(bh)	100 ^(bi)
10, 150	2.4252E+71 ^(bj)	?	150 ^(bk)	150 ^(bl)
10, 200	1.3861E+81 ^(bm)	?	200 ^(bn)	200 ^(bo)
20, 10	3.2308E+19 ^(bp)	2.3414E+21 ^(bq)	10 ^(br)	10 ^(bs)
20, 50	7.9113E+66 ^(bt)	2.6113E+69 ^(bu)	50 ^(bv)	50 ^(bw)
20, 100	1.6334E+107 ^(bx)	?	100 ^(by)	100 ^(bz)
20, 150	2.5424E+138 ^(ca)	?	150 ^(cb)	150 ^(cc)
30, 10	1.0100E+23 ^(cd)	7.6041E+24 ^(ce)	10 ^(cf)	10 ^(cg)
30, 50	6.4510E+83 ^(ch)	?	50 ^(ci)	50 ^(cj)
30, 100	5.7466E+139 ^(ck)	?	100 ^(cl)	100 ^(cm)
30, 150	?	?	?	150
40, 10	3.1162E+25 ^(cn)	?	10 ^(co)	10 ^(cp)
40, 50	1.1273E+96 ^(cq)	?	50 ^(cr)	50 ^(cs)
40, 100	?	?	?	100
40, 150	?	?	?	150
50, 10	2.6757E+27 ^(ct)	?	10 ^(cu)	10 ^(cv)
50, 50	?	?	?	50
50, 100	?	?	?	100
50, 150	?	?	?	150

^(m) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

⁽ⁿ⁾ the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>

^(o) stated by [CÆSAR.BDD](#) version 2.0 on all 29 instances (see all aforementioned scaling parameter values).

^(p) stated by [CÆSAR.BDD](#) version 3.3 to be false on 25 instance(s) out of 29, and unknown on the remaining 4 instance(s).

^(q) stated by [CÆSAR.BDD](#) version 2.0 to be false on 25 instance(s) out of 29, and unknown on the remaining 4 instance(s).

^(r) number of initial tokens, because the net is conservative.

Other properties

CPI (Covered by P-Invariants), CTI (Covered by T-Invariants). All places of this Petri net are N-bounded, i.e. all tokens can gather on any one place. The net enjoys some symmetries.

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- (s) computed at MCC'2014 by Marcie, PNMC, PNXDD, and Stratagem.
 - (t) computed at MCC'2014 by Marcie.
 - (u) computed at MCC'2014 by Marcie and PNMC.
 - (v) computed at MCC'2014 by Marcie and PNMC.
 - (w) computed at MCC'2014 by Marcie and PNMC.
 - (x) computed at MCC'2014 by Marcie.
 - (y) computed at MCC'2014 by Marcie and PNMC.
 - (z) computed at MCC'2014 by Marcie and PNMC.
 - (aa) computed at MCC'2014 by Marcie and PNMC.
 - (ab) computed at MCC'2014 by Marcie.
 - (ac) computed at MCC'2014 by Marcie and PNMC.
 - (ad) computed at MCC'2014 by Marcie and PNMC.
 - (ae) computed at MCC'2014 by Marcie and PNMC.
 - (af) computed at MCC'2014 by Marcie.
 - (ag) computed at MCC'2014 by Marcie and PNMC.
 - (ah) computed at MCC'2014 by Marcie and PNMC.
 - (ai) computed at MCC'2014 by Marcie and PNMC.
 - (aj) computed at MCC'2014 by Marcie.
 - (ak) computed at MCC'2014 by Marcie and PNMC.
 - (al) computed at MCC'2014 by Marcie and PNMC.
 - (am) computed at MCC'2014 by Marcie and PNMC.
 - (an) computed at MCC'2014 by Marcie.
 - (ao) computed at MCC'2014 by Marcie and PNMC.
 - (ap) computed at MCC'2014 by Marcie and PNMC.
 - (aq) computed at MCC'2014 by Marcie and PNMC.
 - (ar) computed at MCC'2014 by Marcie.
 - (as) computed at MCC'2014 by Marcie and PNMC.
 - (at) computed at MCC'2014 by Marcie and PNMC.
 - (au) computed at MCC'2014 by PNMC.
 - (av) computed at MCC'2014 by PNMC.
 - (aw) computed at MCC'2014 by PNMC.
 - (ax) computed at MCC'2014 by Marcie and PNMC.
 - (ay) computed at MCC'2014 by Marcie.
 - (az) computed at MCC'2014 by Marcie and PNMC.
 - (ba) computed at MCC'2014 by Marcie and PNMC.
 - (bb) computed at MCC'2014 by Marcie and PNMC.
 - (bc) computed at MCC'2014 by Marcie.
 - (bd) computed at MCC'2014 by Marcie and PNMC.
 - (be) computed at MCC'2014 by Marcie and PNMC.
 - (bf) computed at MCC'2014 by Marcie and PNMC.
 - (bg) computed at MCC'2014 by Marcie.
 - (bh) computed at MCC'2014 by Marcie and PNMC.
 - (bi) computed at MCC'2014 by Marcie and PNMC.
 - (bj) computed at MCC'2014 by Marcie and PNMC.
 - (bk) computed at MCC'2014 by Marcie and PNMC.
 - (bl) computed at MCC'2014 by Marcie and PNMC.
 - (bm) computed at MCC'2014 by PNMC.
 - (bn) computed at MCC'2014 by PNMC.
 - (bo) computed at MCC'2014 by PNMC.
 - (bp) computed at MCC'2014 by Marcie, PNMC, and PNXDD.
 - (bq) computed at MCC'2014 by Marcie.
 - (br) computed at MCC'2014 by Marcie and PNMC.
 - (bs) computed at MCC'2014 by Marcie and PNMC.
 - (bt) computed at MCC'2014 by Marcie and PNMC.
 - (bu) computed at MCC'2014 by Marcie.
 - (bv) computed at MCC'2014 by Marcie and PNMC.
 - (bw) computed at MCC'2014 by Marcie and PNMC.

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- (bx) computed at MCC'2014 by PNMIC.
 - (by) computed at MCC'2014 by PNMIC.
 - (bz) computed at MCC'2014 by PNMIC.
 - (ca) computed at MCC'2014 by PNMIC.
 - (cb) computed at MCC'2014 by PNMIC.
 - (cc) computed at MCC'2014 by PNMIC.
 - (cd) computed at MCC'2014 by Marcie and PNMIC.
 - (ce) computed at MCC'2014 by Marcie.
 - (cf) computed at MCC'2014 by Marcie and PNMIC.
 - (cg) computed at MCC'2014 by Marcie and PNMIC.
 - (ch) computed at MCC'2014 by PNMIC.
 - (ci) computed at MCC'2014 by PNMIC.
 - (cj) computed at MCC'2014 by PNMIC.
 - (ck) computed at MCC'2014 by PNMIC.
 - (cl) computed at MCC'2014 by PNMIC.
 - (cm) computed at MCC'2014 by PNMIC.
 - (cn) computed at MCC'2014 by PNMIC.
 - (co) computed at MCC'2014 by PNMIC.
 - (cp) computed at MCC'2014 by PNMIC.
 - (cq) computed at MCC'2014 by PNMIC.
 - (cr) computed at MCC'2014 by PNMIC.
 - (cs) computed at MCC'2014 by PNMIC.
 - (ct) computed at MCC'2014 by PNMIC.
 - (cu) computed at MCC'2014 by PNMIC.
 - (cv) computed at MCC'2014 by PNMIC.