

*This form is a summary description of the model entitled “DLCflexbar” proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.*

## Description

The DLC compiler [2,3,4,5] has been developed to automatically generate a distributed implementation of a concurrent system described using the LNT language. The implementation generated by DLC consists of processes (in the C language) executing in parallel and connected with POSIX sockets. These processes synchronize together and communicate using a distributed protocol for value-passing multiway rendezvous. Besides generating a distributed implementation, the DLC compiler can also produce an LNT model of this implementation by combining the source LNT description of the system with the protocol itself [1]. This implementation model can then be used to check the correctness of the distributed implementation using the **CADP** toolbox.

This collection of P/T nets was obtained by using DLC to generate implementation models to various instances of the *FlexibleBarrier* model introduced for the 2017 edition of the MCC. The flexible barrier enables application-wide thread synchronisation in the context of GPU *cooperative kernels* [1]. Each generated LNT model was translated automatically to LOTOS, and then to an interpreted Petri net using the **CADP** toolbox. Finally, a P/T net was obtained by stripping out all data-related information (variables, types, assignments, guards, etc.) from the interpreted Petri net, leading to a NUPN (Nested-Unit Petri Net) model translated to PNML using the **CÆSAR.BDD** tool.

Each instance of the model is parameterized by the maximal number  $N$  of concurrent processes that synchronize on the barrier.

Each instance is also parameterized by its version  $V$ , which specifies how the NUPN has been produced from the LOTOS specification.  $V$  is either equal to “ $a$ ” if the NUPN has been generated *after* applying all the structural and data-flow optimizations of the **CÆSAR** compiler for LOTOS, or to “ $b$ ” if the NUPN has been generated *before* these optimizations.

## References

- [1] Tyler Sorensen, Hugues Evrard, and Alastair F. Donaldson. *Cooperative Kernels: GPU Multitasking for Blocking Algorithms*. Proceedings of the 11th Joint Meeting on Foundations of Software Engineering (ESEC/FSE’17), Paderborn, Germany, pages 431–441. Sept. 2017. Available from <http://multicore.doc.ic.ac.uk/publications/fse-17.html>.
- [2] Hugues Evrard and Frédéric Lang. *Automatic Distributed Code Generation from Formal Models of Asynchronous Concurrent Processes*. Proceedings of the 23rd Euromicro International Conference on Parallel, Distributed and Network-based Processing, Special Session on Formal Approaches to Parallel and Distributed Systems (PDP/4PAD’2015), Turku, Finland. IEEE, 2015. Available from <http://cadp.inria.fr/publications/Evrard-Lang-15.html>.
- [3] Hugues Evrard. *DLC: Compiling a Concurrent System Formal Specification to a Distributed Implementation*. Proceedings of the 22nd International Conference on Tools and Algorithms for the Construction and Analysis of Systems (TACAS’2016), Eindhoven, Netherlands. Springer, 2016. Available from <http://cadp.inria.fr/publications/Evrard-16.html>.
- [4] Hugues Evrard and Frédéric Lang. *Automatic Distributed Code Generation from Formal Models of Asynchronous Processes Interacting by Multiway Rendezvous*. Journal of Logical and Algebraic Methods in Programming, vol. 88, pages 121–153, Elsevier, 2017. Available from <http://cadp.inria.fr/publications/Evrard-Lang-17.html>.
- [5] <http://hevrard.org/DLC>

## Scaling parameter

| Parameter name | Parameter description   | Chosen parameter values                   |
|----------------|---|---|
| $(N, V)$       | $N$ is the number of processes and $V$ is the version defined above | $\{2, 3, 4, 5, 6, 7, 8\} \times \{a, b\}$ |

## Size of the model

| Parameter      | Number of places | Number of transitions | Number of arcs | Number of units | HWB code        |
|----------------|------------------|-----------------------|----------------|-----------------|-----------------|
| $N = 2, V = a$ | 353              | 2169                  | 8205           | 197             | 2-196-249       |
| $N = 2, V = b$ | 4456             | 6272                  | 16411          | 391             | 173-196-1051    |
| $N = 3, V = a$ | 581              | 3891                  | 14956          | 356             | 2-355-431       |
| $N = 3, V = b$ | 7245             | 10555                 | 28284          | 709             | 321-355-1879    |
| $N = 4, V = a$ | 927              | 6615                  | 25705          | 609             | 2-608-715       |
| $N = 4, V = b$ | 11440            | 17128                 | 46731          | 1215            | 559-608-3189    |
| $N = 5, V = a$ | 1415             | 10593                 | 41484          | 980             | 2-979-1125      |
| $N = 5, V = b$ | 17305            | 26483                 | 73264          | 1957            | 911-979-5101    |
| $N = 6, V = a$ | 2069             | 16077                 | 63325          | 1493            | 2-1492-1685     |
| $N = 6, V = b$ | 25104            | 39112                 | 109395         | 2983            | 1401-1492-7735  |
| $N = 7, V = a$ | 2913             | 23319                 | 92260          | 2172            | 2-2171-2419     |
| $N = 7, V = b$ | 35101            | 55507                 | 156636         | 4341            | 2053-2171-11211 |
| $N = 8, V = a$ | 3971             | 32571                 | 129321         | 3041            | 2-3040-3351     |
| $N = 8, V = b$ | 47560            | 76160                 | 216499         | 6079            | 2891-3040-15649 |

## Structural properties

|  |       |
|--|-------|
| <b>ordinary</b> — all arcs have multiplicity one .....   | ✓     |
| <b>simple free choice</b> — all transitions sharing a common input place have no other input place .....                 | ✗ (a) |
| <b>extended free choice</b> — all transitions sharing a common input place have the same input places .....              | ✗ (b) |
| <b>state machine</b> — every transition has exactly one input place and exactly one output place .....                   | ✗ (c) |
| <b>marked graph</b> — every place has exactly one input transition and exactly one output transition .....               | ✗ (d) |
| <b>connected</b> — there is an undirected path between every two nodes (places or transitions) .....                     | ✓ (e) |
| <b>strongly connected</b> — there is a directed path between every two nodes (places or transitions) .....               | ✗ (f) |
| <b>source place(s)</b> — one or more places have no input transitions .....  | ✓ (g) |
| <b>sink place(s)</b> — one or more places have no output transitions .....   | ✗ (h) |
| <b>source transition(s)</b> — one or more transitions have no input places .....   | ✗ (i) |
| <b>sink transitions(s)</b> — one or more transitions have no output places .....   | ✗ (j) |
| <b>loop-free</b> — no transition has an input place that is also an output place .....                                   | ? (k) |
| <b>conservative</b> — for each transition, the number of input arcs equals the number of output arcs .....               | ✗ (l) |
| <b>subconservative</b> — for each transition, the number of input arcs equals or exceeds the number of output arcs ..... | ✗ (m) |
| <b>nested units</b> — places are structured into hierarchically nested sequential units <sup>(n)</sup> .....             | ✓     |

(a) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(b) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(c) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(d) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(e) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(f) from place 1 one cannot reach place 0.

(g) place 0 is a source place.

(h) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(i) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(j) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(k) stated by CÆSAR.BDD version 2.7 to be true on 7 instance(s) out of 14, and false on the remaining 7 instance(s).

(l) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(m) stated by CÆSAR.BDD version 2.7 on all 14 instances (7 values of  $N \times 2$  values of  $V$ ).

(n) the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>

## Behavioural properties

- safe** — *in every reachable marking, there is no more than one token on a place* ..... ✓<sup>(o)</sup>  
**deadlock** — *there exists a reachable marking from which no transition can be fired* ..... ?<sup>(p)</sup>  
**reversible** — *from every reachable marking, there is a transition path going back to the initial marking* ..... ?  
**quasi-live** — *for every transition  $t$ , there exists a reachable marking in which  $t$  can fire* ..... ?<sup>(q)</sup>  
**live** — *for every transition  $t$ , from every reachable marking, one can reach a marking in which  $t$  can fire* ..... ?

## Size of the marking graphs

| Parameter      | Number of reach-able markings | Number of tran-sition firings | Max. number of tokens per place | Max. number of tokens per marking |
|----------------|-------------------------------|-------------------------------|---------------------------------|-----------------------------------|
| $N = 2, V = a$ | $7.97923e+20$ <sup>(r)</sup>  | ?                             | 1                               | 196                               |
| $N = 2, V = b$ | ?                             | ?                             | 1 <sup>(s)</sup>                | $\leq 196$ <sup>(t)</sup>         |
| $N = 3, V = a$ | $2.25393e+30$ <sup>(u)</sup>  | ?                             | 1                               | 355                               |
| $N = 3, V = b$ | ?                             | ?                             | 1 <sup>(v)</sup>                | $\leq 355$ <sup>(w)</sup>         |
| $N = 4, V = a$ | $1.52867e+43$ <sup>(x)</sup>  | ?                             | 1                               | 608                               |
| $N = 4, V = b$ | ?                             | ?                             | 1 <sup>(y)</sup>                | $\leq 608$ <sup>(z)</sup>         |
| $N = 5, V = a$ | ?                             | ?                             | 1                               | 979                               |
| $N = 5, V = b$ | ?                             | ?                             | 1 <sup>(aa)</sup>               | $\leq 979$ <sup>(ab)</sup>        |
| $N = 6, V = a$ | ?                             | ?                             | 1                               | 1492                              |
| $N = 6, V = b$ | ?                             | ?                             | 1 <sup>(ac)</sup>               | $\leq 1492$ <sup>(ad)</sup>       |
| $N = 7, V = a$ | ?                             | ?                             | 1                               | 2171                              |
| $N = 7, V = b$ | ?                             | ?                             | 1 <sup>(ae)</sup>               | $\leq 2171$ <sup>(af)</sup>       |
| $N = 8, V = a$ | ?                             | ?                             | 1 <sup>(ag)</sup>               | 3040                              |
| $N = 8, V = b$ | ?                             | ?                             | 1 <sup>(ah)</sup>               | $\leq 3040$ <sup>(ai)</sup>       |

<sup>(o)</sup> safe by construction – stated by the [CÆSAR](#) compiler.  
<sup>(p)</sup> stated by [CÆSAR.BDD](#) version 2.7 to be false on 6 instance(s) out of 14, and unknown on the remaining 8 instance(s).  
<sup>(q)</sup> stated by [CÆSAR.BDD](#) version 2.7 to be true on 6 instance(s) out of 14, and unknown on the remaining 8 instance(s).  
<sup>(r)</sup> stated by [CÆSAR.BDD](#) version 2.7.  
<sup>(s)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(t)</sup> upper bound given by the number of leaf units.  
<sup>(u)</sup> stated by [CÆSAR.BDD](#) version 2.7.  
<sup>(v)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(w)</sup> upper bound given by the number of leaf units.  
<sup>(x)</sup> stated by [CÆSAR.BDD](#) version 2.7.  
<sup>(y)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(z)</sup> upper bound given by the number of leaf units.  
<sup>(aa)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(ab)</sup> upper bound given by the number of leaf units.  
<sup>(ac)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(ad)</sup> upper bound given by the number of leaf units.  
<sup>(ae)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(af)</sup> upper bound given by the number of leaf units.  
<sup>(ag)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(ah)</sup> stated by the [CÆSAR](#) compiler.  
<sup>(ai)</sup> upper bound given by the number of leaf units.