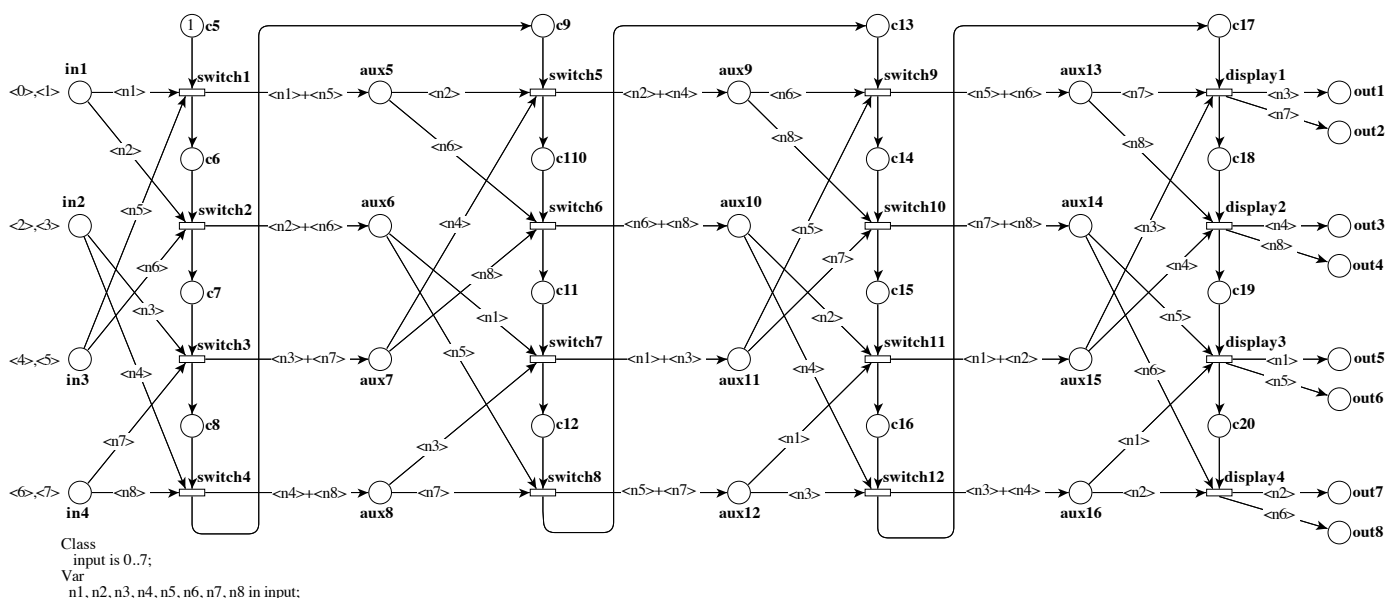


This form is a summary description of the model entitled "Permutation admissibility in multistage interconnection networks" proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

Description

The model describes a 8×8 4 stages shuffle-exchange network. In order to ease readability, the net components are grouped in columns similar to the way the switches are arranged in stages. Thus, whole net is represented as a cascade of columns alternating in type of the components being either place or transition. Transitions occur column-wise from the leftmost to the rightmost and in columns from the topmost to the bottommost. It can be easily seen that no token can visit a place more than once. Direction of the arcs indicates the flow of tokens through the net.

Here, we consider the scaling parameter N as a multiplier for the initial marking in places $\text{in}\langle x \rangle$ and c5 . The figure shows the model when $N = 1$.



Graphical representation for $N = 1$

References

R. Bashirov, F. Kordon, and H. Lort. Exploiting colored Petri nets to decide on permutation admissibility. *Acta Informatica*, 46(1):43–55, February 2009.

Scaling parameter

| Parameter name | Parameter description | Chosen parameter values |
|----------------|---|-------------------------|
| N | Multiplier for the marking of places $\text{in}\langle x \rangle$ and c5 | 1, 2, 5, 10, 20, 50 |

Size of the model

Although the model is parameterized, its size does not depend on parameter values.

number of places: 40
 number of transitions: 16
 number of arcs: 83

Structural properties

| | | |
|--|-------|-------|
| ordinary — all arcs have multiplicity one | | X |
| simple free choice — all transitions sharing a common input place have no other input place | | X (a) |
| extended free choice — all transitions sharing a common input place have the same input places | | X (b) |
| state machine — every transition has exactly one input place and exactly one output place | | X (c) |
| marked graph — every place has exactly one input transition and exactly one output transition | | X (d) |
| connected — there is an undirected path between every two nodes (places or transitions) | | ✓ (e) |
| strongly connected — there is a directed path between every two nodes (places or transitions) | | X (f) |
| source place(s) — one or more places have no input transitions | | ✓ (g) |
| sink place(s) — one or more places have no output transitions | | ✓ (h) |
| source transition(s) — one or more transitions have no input places | | X (i) |
| sink transitions(s) — one or more transitions have no output places | | X (j) |
| loop-free — no transition has an input place that is also an output place | | ✓ (k) |
| conservative — for each transition, the number of input arcs equals the number of output arcs | | X (l) |
| subconservative — for each transition, the number of input arcs equals or exceeds the number of output arcs | | X (m) |
| nested units — places are structured into hierarchically nested sequential units ⁽ⁿ⁾ | | X |

Behavioural properties

| | | |
|--|-------|-------|
| safe — in every reachable marking, there is no more than one token on a place | | X (o) |
| deadlock — there exists a reachable marking from which no transition can be fired | | ✓ (p) |
| reversible — from every reachable marking, there is a transition path going back to the initial marking | | X |
| quasi-live — for every transition t , there exists a reachable marking in which t can fire | | ? |
| live — for every transition t , from every reachable marking, one can reach a marking in which t can fire | | ? |

(a) the net is not ordinary in all its 6 instances (1, 2, 5, 10, 20, and 50).
 (b) the net is not ordinary in all its 6 instances (1, 2, 5, 10, 20, and 50).
 (c) the net is not ordinary in all its 6 instances (1, 2, 5, 10, 20, and 50).
 (d) the net is not ordinary in all its 6 instances (1, 2, 5, 10, 20, and 50).
 (e) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (f) from place “aux16_0” one cannot reach place “in4_6”.
 (g) there exist 9 source places, e.g., place “in4_6”.
 (h) there exist 64 sink places, e.g., place “out7_1”.
 (i) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (j) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (k) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (l) stated by [PNML2NUPN](#) 1.3.0 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (m) stated by [PNML2NUPN](#) 1.3.0 on all 6 instances (1, 2, 5, 10, 20, and 50).
 (n) the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>
 (o) in the initial marking, some places have several tokens (the number of which depends on N).
 (p) confirmed at MCC’2014 by Helena on all 6 colored instances, and by Lola and Tapaal on all 6 P/T instances.

Size of the marking graphs

| Parameter | Number of reachable markings | Number of transition firings | Max. number of tokens per place | Max. number of tokens per marking |
|-----------|------------------------------|------------------------------|---------------------------------|-----------------------------------|
| $N = 1$ | 52 537 ^(q) | 54 600 ^(r) | 1 ^(s) | 9 ^(t) |
| $N = 2$ | ? | ? | ? | ≥ 18 |
| $N = 5$ | ? | ? | ? | ≥ 45 |
| $N = 10$ | ? | ? | ? | ≥ 90 |
| $N = 20$ | ? | ? | ? | ≥ 180 |
| $N = 50$ | ? | ? | ? | ≥ 450 |

^(q) Computed by Alpina, and ITS-Tools at MCC'2013; confirmed at MCC'2014 by Helena on the colored net instance, and by GreatSPN, Marcie, PNMC, PNXDD, and Tapaal on the P/T net instance.

^(r) computed at MCC'2014 by Helena on the colored net instance, and by Marcie on the P/T net instance.

^(s) computed at MCC'2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.

^(t) computed at MCC'2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.