This form is a summary description of the model entitled “Peterson” proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

Description

This is a model of the Peterson’s algorithm for the mutual exclusion problem, in its generalized version for N processes. This algorithm is based on shared memory communication and uses a loop with N-1 iterations, each iteration is in charge of stopping one of the competing processes.

Graphical representation for N = 2

References

http://dblp.uni-trier.de/rec/bibtex/journals/ipl/Peterson81
Scaling parameter

<table>
<thead>
<tr>
<th>Parameter name</th>
<th>Parameter description</th>
<th>Chosen parameter values</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N$</td>
<td>$N$ is the number of processes. It has an impact on the initial marking of places Idle, Turn and WantSection. It has, also, an impact on the guards of transitions ProgressTurn and Loop. The color functions between EndTurn and AccessCS, as well as the one between IsEndLoop and EndLoop are impacted.</td>
<td>2, 3, 4, 5, 6, 7</td>
</tr>
</tbody>
</table>

Size of the colored net model

- number of places: 11
- number of transitions: 14
- number of arcs: 42

Size of the derived P/T model instances

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Number of places</th>
<th>Number of transitions</th>
<th>Number of arcs</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N = 2$</td>
<td>102</td>
<td>126</td>
<td>384</td>
</tr>
<tr>
<td>$N = 3$</td>
<td>244</td>
<td>332</td>
<td>1016</td>
</tr>
<tr>
<td>$N = 4$</td>
<td>480</td>
<td>690</td>
<td>2120</td>
</tr>
<tr>
<td>$N = 5$</td>
<td>834</td>
<td>1242</td>
<td>3828</td>
</tr>
<tr>
<td>$N = 6$</td>
<td>1330</td>
<td>2030</td>
<td>6272</td>
</tr>
<tr>
<td>$N = 7$</td>
<td>1992</td>
<td>3096</td>
<td>9584</td>
</tr>
</tbody>
</table>

Structural properties

- ordinary — all arcs have multiplicity one
- simple free choice — all (different) transitions with a shared input place have no other input place
- state machine — every transition has exactly one input place and exactly one output place
- marked graph — every place has exactly one input transition and exactly one output transition
- connected — there is an undirected path between every two nodes (places or transitions)
- strongly connected — there is a directed path between every two nodes (places or transitions)
- source place(s) — one or more places have no input transitions
- sink place(s) — one or more places have no output transitions
- source transition(s) — one or more transitions have no input places
- sink transition(s) — one or more transitions have no output places
- loop-free — no transition has an input place that is also an output place
- conservative — for each transition, the number of input arcs equals the number of output arcs
- subconservative — for each transition, the number of input arcs equals or exceeds the number of output arcs

(a) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(b) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(c) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(d) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(e) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(f) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(g) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(h) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(i) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
(j) stated by CÆSAR.BDD version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).
Model: Peterson  
Type: Colored Net (with derived P/T Nets)  
Origin: Academic

since MCC 2011
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nested units — places are structured into hierarchically nested sequential units

Behavioural properties

safe — in every reachable marking, there is no more than one token on a place

deadlock — there exists a reachable marking from which no transition can be fired

reversible — from every reachable marking, there is a transition path going back to the initial marking

quasi-live — for every transition t, there exists a reachable marking in which t can fire

live — for every transition t, from every reachable marking, one can reach a marking in which t can fire

Size of the marking graphs

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Number of reachable markings</th>
<th>Number of transition firings</th>
<th>Max. number of tokens per place</th>
<th>Max. number of tokens per marking</th>
</tr>
</thead>
<tbody>
<tr>
<td>N = 2</td>
<td>20,754 (q)</td>
<td>62,262 (q)</td>
<td>1 (w)</td>
<td>8 (q)</td>
</tr>
<tr>
<td>N = 3</td>
<td>3,408 \times 10^6 (u)</td>
<td>1,363 \times 10^4 (v)</td>
<td>?</td>
<td>?</td>
</tr>
<tr>
<td>N = 4</td>
<td>6,299 \times 10^9 (y)</td>
<td>?</td>
<td>?</td>
<td>\geq 14</td>
</tr>
<tr>
<td>N = 5</td>
<td>1,366 \times 10^{11} (z)</td>
<td>?</td>
<td>?</td>
<td>\geq 17</td>
</tr>
<tr>
<td>N = 6</td>
<td>?</td>
<td>?</td>
<td>?</td>
<td>\geq 20</td>
</tr>
<tr>
<td>N = 7</td>
<td>?</td>
<td>?</td>
<td>?</td>
<td>\geq 23</td>
</tr>
</tbody>
</table>

(m) the definition of Nested-Unit Petri Nets (NUPN) is available from http://mcc.lip6.fr/nupn.php
(n) stated by CÆSAR.BDD version 2.0 to be true on 1 instance(s) out of 6, and unknown on the remaining 5 instance(s).
(o) stated by CÆSAR.BDD version 2.0 to be false on 1 instance(s) out of 6, and unknown on the remaining 5 instance(s); confirmed at MCC’2014 by Helena on 3 colored instances (N = 2, N = 3, and N = 4), and by GreatSPN, Lola, and/or Tapaal on the 3 corresponding P/T instances.
(p) found to be true by CÆSAR.BDD version 1.9 on instances 2 and 3.
(q) computed at MCC’2013 by Alpina, ITS-Tools, Marcie, Neco, and PNXDD; confirmed by CÆSAR.BDD version 1.8; confirmed at MCC’2014 by Helena on the colored net instance, and by GreatSPN, Marcie, PNMC, PNXDD, Stratagem, and Tapaal on the P/T net instance.
(r) computed at MCC’2014 by Helena on the colored net instance and by Marcie on the P/T net instance.
(s) confirmed at MCC’2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.
(t) computed at MCC’2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.
(u) computed at MCC’2013 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.  
(v) computed at MCC’2014 by Helena on the colored net instance, and by GreatSPN, Marcie, PNMC, and PNXDD on the P/T net instance.
(w) computed at MCC’2014 by GreatSPN, Marcie, and PNMC on the P/T net instance.
(x) computed at MCC’2014 by GreatSPN, Marcie, and PNMC on the P/T net instance.
(y) computed at MCC’2013 by GreatSPN, Marcie, and PNMC on the P/T net instance.
(z) computed at MCC’2013 by ITS-Tools, and PNXDD.
(a) computed at MCC’2013 by ITS-Tools.