



## Scaling parameter

Parameter name	Parameter description	Chosen parameter values
$N$	$N$ is the number of processes. It has an impact on the initial marking of places Idle, Turn and WantSection. It has, also, an impact on the guards of transitions ProgressTurn and Loop. The color functions between EndTurn and AccessCS, as well as the one between IsEndLoop and EndLoop are impacted.	2, 3, 4, 5, 6, 7

## Size of the colored net model

number of places: 11  
 number of transitions: 14  
 number of arcs: 42

## Size of the derived P/T model instances

Parameter	Number of places	Number of transitions	Number of arcs
$N = 2$	102	126	384
$N = 3$	244	332	1016
$N = 4$	480	690	2120
$N = 5$	834	1242	3828
$N = 6$	1330	2030	6272
$N = 7$	1992	3096	9584

## Structural properties

- ordinary** — *all arcs have multiplicity one* ..... ✓
- simple free choice** — *all (different) transitions with a shared input place have no other input place* ..... ✗ (a)
- state machine** — *every transition has exactly one input place and exactly one output place* ..... ✗ (b)
- marked graph** — *every place has exactly one input transition and exactly one output transition* ..... ✗ (c)
- connected** — *there is an undirected path between every two nodes (places or transitions)* ..... ✓ (d)
- strongly connected** — *there is a directed path between every two nodes (places or transitions)* ..... ✓ (e)
- source place(s)** — *one or more places have no input transitions* ..... ✗ (f)
- sink place(s)** — *one or more places have no output transitions* ..... ✗ (g)
- source transition(s)** — *one or more transitions have no input places* ..... ✗ (h)
- sink transitions(s)** — *one or more transitions have no output places* ..... ✗ (i)
- loop-free** — *no transition has an input place that is also an output place* ..... ✗ (j)
- conservative** — *for each transition, the number of input arcs equals the number of output arcs* ..... ✓ (k)
- subconservative** — *for each transition, the number of input arcs equals or exceeds the number of output arcs* ..... ✓ (l)

(a) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (b) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (c) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (d) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (e) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (f) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (g) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (h) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (i) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (j) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (k) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).  
 (l) stated by [CÆSAR.BDD](#) version 1.7 on all 6 instances (2, 3, 4, 5, 6, and 7).

nested units — places are structured into hierarchically nested sequential units <sup>(m)</sup> ..... X

## Behavioural properties

safe — in every reachable marking, there is no more than one token on a place ..... ✓ <sup>(n)</sup>  
 deadlock — there exists a reachable marking from which no transition can be fired ..... X <sup>(o)</sup>  
 reversible — from every reachable marking, there is a transition path going back to the initial marking ..... ✓  
 quasi-live — for every transition  $t$ , there exists a reachable marking in which  $t$  can fire ..... ? <sup>(p)</sup>  
 live — for every transition  $t$ , from every reachable marking, one can reach a marking in which  $t$  can fire ..... ?

## Size of the marking graphs

Parameter	Number of reachable markings	Number of transition firings	Max. number of tokens per place	Max. number of tokens per marking
$N = 2$	20 754 <sup>(q)</sup>	62 262 <sup>(r)</sup>	1 <sup>(s)</sup>	8 <sup>(t)</sup>
$N = 3$	$3.408 \times 10^6$ <sup>(u)</sup>	$1.363 \times 10^7$ <sup>(v)</sup>	1 <sup>(w)</sup>	11 <sup>(x)</sup>
$N = 4$	$6.299 \times 10^8$ <sup>(y)</sup>	?	?	$\geq 14$
$N = 5$	$1.366 \times 10^{11}$ <sup>(z)</sup>	?	?	$\geq 17$
$N = 6$	?	?	?	$\geq 20$
$N = 7$	?	?	?	$\geq 23$

<sup>(m)</sup>the definition of Nested-Unit Petri Nets (NUPN) is available from <http://mcc.lip6.fr/nupn.php>

<sup>(n)</sup> stated by CÆSAR.BDD version 2.0 to be true on 1 instance(s) out of 6, and unknown on the remaining 5 instance(s).

<sup>(o)</sup> stated by CÆSAR.BDD version 2.0 to be false on 1 instance(s) out of 6, and unknown on the remaining 5 instance(s); confirmed at MCC'2014 by Helena on 3 colored instances ( $N = 2$ ,  $N = 3$ , and  $N = 4$ ), and by GreatSPN, Lola, and/or Tapaal on the 3 corresponding P/T instances.

<sup>(p)</sup> found to be true by CÆSAR.BDD version 1.9 on instances 2 and 3.

<sup>(q)</sup> computed at MCC'2013 by Alpina, ITS-Tools, Marcie, Neco, and PNXDD; confirmed by CÆSAR.BDD version 1.8; confirmed at MCC'2014 by Helena on the colored net instance, and by GreatSPN, Marcie, PNMC, PNXDD, Stratagem, and Tapaal on the P/T net instance.

<sup>(r)</sup> computed at MCC'2014 by Helena on the colored net instance and by Marcie on the P/T net instance.

<sup>(s)</sup> confirmed at MCC'2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.

<sup>(t)</sup> computed at MCC'2014 by GreatSPN, Marcie, PNMC, and Tapaal on the P/T net instance.

<sup>(u)</sup> computed at MCC'2013 by Alpina, ITS-Tools, Marcie, and PNXDD; confirmed by CÆSAR.BDD version 1.8; confirmed at MCC'2014 by Helena on the colored net instance, and by GreatSPN, Marcie, PNMC, and PNXDD on the P/T net instance.

<sup>(v)</sup> computed at MCC'2014 by Helena on the colored net instance, and by Marcie on the P/T net instance.

<sup>(w)</sup> computed at MCC'2014 by GreatSPN, Marcie, and PNMC on the P/T net instance.

<sup>(x)</sup> computed at MCC'2014 by GreatSPN, Marcie, and PNMC on the P/T net instance.

<sup>(y)</sup> computed at MCC'2013 by ITS-Tools, and PNXDD.

<sup>(z)</sup> computed at MCC'2013 by ITS-Tools.