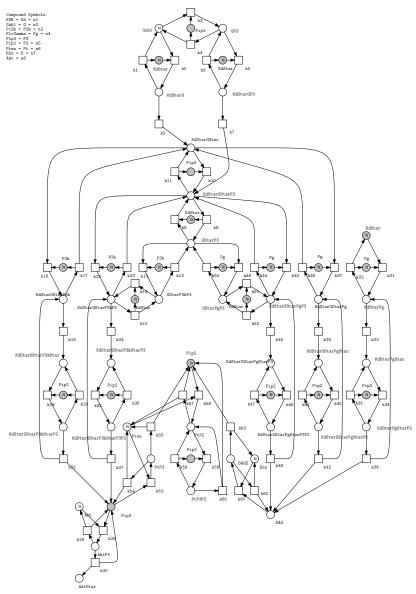
This form is a summary description of the model entitled "Angiogenesis" proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

#### Description

Angiogenesis, defined as the formation of new vessels from the existing ones, is a topic of great interest in all areas of human biology, particularly to scientists studying vascular development, vascular malformation and cancer biology. Angiogenesis is a complex process involving the activities of many growth factors and relative receptors, which trigger several signaling pathways resulting in different cellular responses. The Petri net was introduced in [1] and refined in [2].



Graphical representation with parameter N. The gray coloured places are logic/fusion places.

#### References

- 1 L. Napione, D. Manini, F. Cordero, A. Horvath, A. Picco, M. D. Pierro, S. Pavan, M. Sereno, A. Veglio, F. Bussolino, and G. Balbo. On the Use of Stochastic Petri Nets in the Analysis of Signal Transduction Pathways for Angiogenesis Process. In Proc. CMSB 2009, pages 281295. LNCS/LNBI 5688, Springer, 2009.
- 2 F. Cordero, A. Horvath, D. Manini, L. Napione, M. D. Pierro, S. Pavan, A. Picco, A. Veglio, M. Sereno, F. Bussolino, and G. Balbo. Simplification of a complex signal transduction model using invariants and flow equivalent servers. Theor. Comput. Sci., 412(43):6036-6057, 2011.

## Scaling parameter

Parameter name	Parameter description	Chosen parameter values
N	initial number of tokens on places Akt, Enz,	1, 5, 10, 15, 20, 25, 50
	Gab1, KdStar, P3k, Pg, Pip2 and Pten	

#### Size of the model

Although the model is parameterized, its size does not depend on parameter values.

number of places: 39 number of transitions: 64 number of arcs: 185

### Structural properties

	<b>. /</b> .
simple free choice — all (different) transitions with a shared input place have no other input place	<b>X</b> (a)
but in the configuration of the country of the tripular place with the country of	<b>X</b> (b)
marked graph — every place has exactly one input transition and exactly one output transition	<b>X</b> (c)
connected — there is an undirected path between every two nodes (places or transitions)	<b>√</b> (d)
strongly connected — there is a directed path between every two nodes (places or transitions)	<b>X</b> (e)
source place(s) — one or more places have no input transitions	<b>X</b> (f)
sink place(s) — one or more places have no output transitions	<b>(</b> g)
source transition(s) — one or more transitions have no input places	<b>X</b> (h)
sink transitions(s) — one or more transitions have no output places	<b>X</b> (i)
loop-free — no transition has an input place that is also an output place	<b>√</b> (j)
conservative — for each transition, the number of input arcs equals the number of output arcs	<b>X</b> (k)
subconservative — for each transition, the number of input arcs equals or exceeds the number of output arcs	<b>X</b> (1)
nested units — places are structured into hierarchically nested sequential units (m)	

<sup>(</sup>a) 40 arcs are not free choice, e.g., the arc from place "p6" (which has 2 outgoing transitions) to transition "t0" (which has 2 input places).

<sup>(</sup>b) 57 transitions are not of a state machine, e.g., transition "t0".

 $<sup>^{\</sup>rm (c)}$  38 places are not of a marked graph, e.g., place "p5".

<sup>(</sup>d) stated by CÆSAR.BDD version 2.0 on all 7 instances (1, 5, 10, 15, 20, 25, and 50).

<sup>(</sup>e) from place "p2" one cannot reach place "p0".

<sup>(</sup>f) stated by CÆSAR.BDD version 2.0 on all 7 instances (1, 5, 10, 15, 20, 25, and 50).

<sup>(</sup>g) place "p2" is a sink place.

<sup>(</sup>h) stated by CÆSAR.BDD version 2.0 on all 7 instances (1, 5, 10, 15, 20, 25, and 50).

<sup>(</sup>i) stated by CÆSAR.BDD version 2.0 on all 7 instances (1, 5, 10, 15, 20, 25, and 50).

<sup>(</sup>j) stated by CÆSAR.BDD version 2.0 on all 7 instances (1, 5, 10, 15, 20, 25, and 50).

<sup>(</sup>k) 57 transitions are not conservative, e.g., transition "t0".

<sup>(1) 33</sup> transitions are not subconservative, e.g., transition "t1".

<sup>(</sup>m) the definition of Nested-Unit Petri Nets (NUPN) is available from http://mcc.lip6.fr/nupn.php

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## Behavioural properties

safe — in every reachable marking, there is no more than one token on a place	? (	n)
deadlock — there exists a reachable marking from which no transition can be fired	<u>/ (</u>	0)
reversible — from every reachable marking, there is a transition path going back to the initial marking	<b>(</b>	p)
quasi-live — for every transition t, there exists a reachable marking in which t can fire		
live — for every transition t, from every reachable marking, one can reach a marking in which t can fire	<b>K</b> (	$\mathbf{q}$

#### Size of the marking graphs

Parameter	Number of reachable	Number of tran-	Max. number of	Max. number of
	markings	sition firings	tokens per place	tokens per marking
N=1	110 <sup>(r)</sup>	288 <sup>(s)</sup>	$N^{(t)}$	8 (u)
N=5	$4.2735E + 7^{(v)}$	4.8687E+8 (w)	$N^{(\mathbf{x})}$	40 <sup>(y)</sup>
N = 10	8.2265E+11 <sup>(z)</sup>	1.5636E + 13 (aa)	$N^{\mathrm{(ab)}}$	80 <sup>(ac)</sup>
N = 15	1 115 538 966 669 107 <sup>(ad)</sup>	?	N	$\geq 120$
N = 20	$351820047967344849^{\mathrm{(ae)}}$	?	N	≥ 160
N = 25	$43090329340850957348^{\text{(af)}}$	?	N	≥ 200
N = 50	?	?	N	$\geq 400$

<sup>(</sup>n) stated by CÆSAR.BDD version 2.0 to be true on 1 instance(s) out of 7, and false on the remaining 6 instance(s).

<sup>(</sup>o) Checked by Marcie on 2013-12-13; confirmed at MCC'2014 by Tapaal on 2 instances and by Lola on 5 instances.

<sup>(</sup>p) has dead states.

<sup>(</sup>q) has dead states.

<sup>(</sup>r) given in [2] and computed by Marcie on 2013-12-13; confirmed by CÆSAR.BDD version 2.0; confirmed at MCC'2014 by Marcie, PNMC, PNXDD, Stratagem, and Tapaal.

<sup>(</sup>s) computed at MCC'2014 by Marcie.

 $<sup>^{\</sup>rm (t)}$  confirmed at MCC'20214 by Marcie, PNMC, and Tapaal.

<sup>(</sup>u) computed at MCC'2014 by Marcie, PNMC, and Tapaal.

<sup>(</sup>v) exact value 42 734 935 given in [2] and computed by Marcie on 2013-12-13; confirmed at MCC'2014 by Marcie, PNMC, and PNXDD.

 $<sup>^{\</sup>rm (w)}$  computed at MCC'2014 by Marcie.

 $<sup>^{(\</sup>mathrm{x})}$  confirmed at MCC'2014 by Marcie and PNMC.

 $<sup>^{\</sup>rm (y)}$  computed at MCC'2014 by Marcie and PNMC.

<sup>(</sup>z) exact value 822 645 885 495 computed by Marcie on 2013-12-13; confirmed at MCC'2014 by Marcie, PNMC, and PNXDD.

 $<sup>^{\</sup>rm (aa)}$  computed at MCC'2014 by Marcie.

<sup>(</sup>ab) confirmed at MCC'2014 by Marcie and PNMC.

 $<sup>^{(</sup>ac)}$  computed at MCC'2014 by Marcie and PNMC.

 $<sup>^{(</sup>ad)}$  computed by Marcie on 2013-12-13.

 $<sup>^{(</sup>ae)}$  computed by Marcie on 2013-12-13.

<sup>(</sup>af) computed by Marcie on 2013-12-13.