This form is a summary description of the model entitled "Discovery GPU" proposed for the Model Checking Contest @ Petri Nets. Models can be given in several instances parameterized by scaling parameters. Colored nets can be accompanied by one or many equivalent, unfolded P/T nets. Models are given together with property files (possibly, one per model instance) giving a set of properties to be checked on the model.

## Description

This model describes the discovery protocol [1] used to dynamically detect the amount of thread workgroups that can be scheduled at the same time on a given GPU, for a given application. Each workgroup participate in a mutex-protected poll, which is closed once a workgroup is able to re-visit the poll. All workgroups that were able to participate in the poll are thus actually running in parallel on different hardware-level compute-units. As GPUs have non-preemptive scheduling, these discovered workgroups are able to safely participate in blocking synchronisation. This protocol is critical to enable safe inter-workgroup blocking synchronisation, which in turn can provide significant performance improvements in some applications.

The discovery protocol was formally specified using the LNT value-passing process calculus and analyzed using the verification tools available in the CADP toolbox. The collection of P/T nets was obtained from the LNT specifications of the protocol. Each LNT specification was translated automatically to LOTOS, and then to an interpreted Petri net using the CADP toolbox. Finally, a P/T net was obtained by stripping out all data-related information (variables, types, assignments, guards, etc.) from the interpreted Petri net, leading to a NUPN (Nested-Unit Petri Net) model translated to PNML using the CÆSAR.BDD tool.

Each instance of the model is parameterized by the number N of threads.

Each instance is also parameterized by its version V, which specifies how the NUPN has been produced from the LOTOS specification. V is either equal to "a" if the NUPN has been generated *after* applying all the structural and data-flow optimizations of the CÆSAR compiler for LOTOS, or to "b" if the NUPN has been generated *before* these optimizations.

## References

[1] Tyler Sorensen, Alastair F. Donaldson, Mark Batty, Ganesh Gopalakrishnan, and Zvonimir Rakamaric. Portable Interworkgroup Barrier Synchronisation for GPUs. In Proc. of the 31st Annual ACM SIGPLAN Conference on Object-Oriented Programming, Systems, Languages, and Applications (OOPSLA'16), Amsterdam, The Netherlands, November 2016.

## Scaling parameter

Parameter name	Parameter description	Chosen parameter values	
(N,V)	N is the number of threads and $V$ is the	$\{6,, 15\} \times \{a, b\}$	
	version defined above		

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Size of the model
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Parameter	Number of	Number of	Number of	Number of	HWB code
	places	transitions	arcs	units	
N = 06, V = a	63	85	273	9	2-8-27
N = 06, V = b	184	194	503	15	7-8-44
N = 07, V = a	73	99	318	10	2-9-31
N = 07, V = b	212	224	582	17	8-9-50
N = 08, V = a	83	113	363	11	2-10-35
N = 08, V = b	240	254	661	19	9-10-56
N = 09, V = a	93	127	408	12	2-11-39
N = 09, V = b	268	284	740	21	10-11-62
N = 10, V = a	103	141	453	13	2-12-43
N = 10, V = b	296	314	819	23	11-12-68
N = 11, V = a	113	155	498	14	2-13-47
N = 11, V = b	324	344	898	25	12-13-74
N = 12, V = a	123	169	543	15	2-14-51
N = 12, V = b	352	374	977	27	13-14-80
N = 13, V = a	133	183	588	16	2-15-55
N = 13, V = b	380	404	1056	29	14-15-86
N = 14, V = a	143	197	633	17	2-16-59
N = 14, V = b	408	434	1135	31	15 - 16 - 92
N = 15, V = a	153	211	678	18	2-17-63
N = 15, V = b	436	464	1214	33	16-17-98

### Structural properties

ordinary — all arcs have multiplicity one	🖌
simple free choice — all transitions sharing a common input place have no other input place	<b>X</b> (a)
extended free choice — all transitions sharing a common input place have the same input places	<b>X</b> (b)
state machine — every transition has exactly one input place and exactly one output place	<b>X</b> (c)
marked graph — every place has exactly one input transition and exactly one output transition	<b>X</b> (d)
connected — there is an undirected path between every two nodes (places or transitions)	🖌 (e)
strongly connected — there is a directed path between every two nodes (places or transitions)	<b>X</b> (f)
source place(s) — one or more places have no input transitions $\dots$	🖌 (g)
sink place(s) — one or more places have no output transitions	.? <sup>(h)</sup>
source transition(s) — one or more transitions have no input places	<b>X</b> (i)
sink transitions(s) — one or more transitions have no output places $\dots$	. ? <mark>(j</mark> )
loop-free — no transition has an input place that is also an output place	. ? (k)
conservative — for each transition, the number of input arcs equals the number of output arcs	<b>X</b> (l)
subconservative — for each transition, the number of input arcs equals or exceeds the number of output arcs	<b>X</b> (m)
<b>nested units</b> — places are structured into hierarchically nested sequential units <sup>(n)</sup>	🗸

<sup>&</sup>lt;sup>(a)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>&</sup>lt;sup>(b)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>&</sup>lt;sup>(c)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>&</sup>lt;sup>(d)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>&</sup>lt;sup>(e)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

 $<sup>^{\</sup>rm (f)}$  from place 1 one cannot reach place 0.

<sup>&</sup>lt;sup>(g)</sup> place 0 is a source place.

<sup>&</sup>lt;sup>(h)</sup> stated by CÆSAR.BDD version 2.7 to be true on 10 instance(s) out of 20, and false on the remaining 10 instance(s).

<sup>&</sup>lt;sup>(i)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>(</sup>j) stated by CÆSAR.BDD version 2.7 to be true on 10 instance(s) out of 20, and false on the remaining 10 instance(s).

<sup>&</sup>lt;sup>(k)</sup> stated by CÆSAR.BDD version 2.7 to be true on 10 instance(s) out of 20, and false on the remaining 10 instance(s).

<sup>&</sup>lt;sup>(1)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>&</sup>lt;sup>(m)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

 $<sup>\</sup>label{eq:linear} \ensuremath{^{(n)}}\ensuremath{$ 

## Behavioural properties

$\mathbf{safe} - in \ every \ reachable \ marking, \ there \ is \ no \ more \ than \ one \ token \ on \ a \ place \ \dots \dots$	🖌 (o)
dead place(s) — one or more places have no token in any reachable marking $\dots$	<b>X</b> (p)
dead transition(s) — one or more transitions cannot fire from any reachable marking	<b>X</b> (q)
deadlock — there exists a reachable marking from which no transition can be fired	? (r)
reversible — from every reachable marking, there is a transition path going back to the initial marking	.? <sup>(s)</sup>
live — for every transition t, from every reachable marking, one can reach a marking in which t can fire	.? <sup>(t)</sup>

#### Size of the marking graphs

	Number of reach-	Number of tran-	Max. number of	Max. number of
Parameter	able markings	sition firings	tokens per place	tokens per marking
N = 06, V = a	$1.77156e + 06^{(u)}$	?	1	8
N = 06, V = b	$6.13871e + 09^{(v)}$	?	1	8
N = 07, V = a	1.94872e + 07 <sup>(w)</sup>	?	1	9
N = 07, V = b	$\geq 1.59038e + 11^{(x)}$	?	1 (y)	9
N = 08, V = a	$2.14359e + 08^{(z)}$	?	1	10
N = 08, V = b	$\geq 4.16622e + 11$ (aa)	?	$1^{(ab)}$	10
N = 09, V = a	$2.35795e+09^{(ac)}$	?	1	11
N = 09, V = b	$\geq 1.44163e + 12^{\text{(ad)}}$	?	1	11
N = 10, V = a	$2.59374e+10^{(ae)}$	?	1	12
N = 10, V = b	$\geq 5.47101e + 12^{\text{(af)}}$	?	$1^{(ag)}$	12
N = 11, V = a	2.85312e+11 <sup>(ah)</sup>	?	1	13
N = 11, V = b	$\geq 1.61943e + 13$ <sup>(ai)</sup>	?	1 (aj)	13
N = 12, V = a	$3.13843e+12^{(ak)}$	?	1	14
N = 12, V = b	$\geq 3.85496e + 13^{(al)}$	?	$1^{(am)}$	14
N = 13, V = a	3.45227e+13 <sup>(an)</sup>	?	1	15
N = 13, V = b	$\geq 7.55166e + 13$ <sup>(ao)</sup>	?	1 <sup>(ap)</sup>	15
N = 14, V = a	$3.7975e+14^{(aq)}$	?	1	16
N = 14, V = b	$\geq 1.23851e + 14^{(ar)}$	?	$1^{(as)}$	16
N = 15, V = a	$4.17725e+15^{(at)}$	?	1	17
N = 15, V = b	$\geq 4.73641e + 14^{(au)}$	?	$1^{(av)}$	17

<sup>(o)</sup> safe by construction – stated by the CÆSAR compiler.

<sup>(p)</sup> stated by CÆSAR.BDD version 3.3 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>(q)</sup> stated by CÆSAR.BDD version 2.7 on all 20 instances (10 values of  $N \times 2$  values of V).

<sup>(r)</sup> stated by CÆSAR.BDD version 2.7 to be true on 11 instance(s) out of 20, and unknown on the remaining 9 instance(s).

(s) stated by CÆSAR.BDD version 2.7 to be false on 11 instance(s) out of 20, and unknown on the remaining 9 instance(s).

(t) stated by CÆSAR.BDD version 2.7 to be false on 11 instance(s) out of 20, and unknown on the remaining 9 instance(s).

- $^{(u)}$  stated by CÆSAR.BDD version 2.7.
- (v) stated by CÆSAR.BDD version 2.7.
- <sup>(w)</sup> stated by CÆSAR.BDD version 2.7.
- $^{(x)}$  stated by CÆSAR.BDD version 2.7.
- $^{(\mathrm{y})}$  stated by the CÆSAR compiler.
- $^{(z)}$  stated by CÆSAR.BDD version 2.7.
- $^{(aa)}$  stated by CÆSAR.BDD version 2.7.
- (ab) stated by the CÆSAR compiler.
- (ac) stated by CÆSAR.BDD version 2.7.
- (ad) stated by CÆSAR.BDD version 2.7. (ae) stated by CÆSAR.BDD version 2.7.
- (af) stated by CÆSAR.BDD version 2.7.
- <sup>(ag)</sup> stated by the CÆSAR compiler.
- <sup>(ah)</sup> stated by CÆSAR.BDD version 2.7.
- <sup>(ai)</sup> stated by CÆSAR.BDD version 2.7.
- <sup>(aj)</sup> stated by the CÆSAR compiler.
- (ak) stated by CÆSAR.BDD version 2.7.
- <sup>(al)</sup> stated by CÆSAR.BDD version 2.7. <sup>(am)</sup> stated by the CÆSAR compiler.

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- $^{(ap)}$  stated by the CÆSAR compiler. (aq) stated by CÆSAR.BDD version 2.7.
- <sup>(ar)</sup> stated by CÆSAR.BDD version 2.7.  $^{\rm (as)}$  stated by the CÆSAR compiler.
- <sup>(at)</sup> stated by CÆSAR.BDD version 2.7.
- <sup>(au)</sup> stated by CÆSAR.BDD version 2.7.

 $<sup>^{\</sup>rm (an)}$  stated by CÆSAR.BDD version 2.7.

<sup>(</sup>ao) stated by CÆSAR.BDD version 2.7.

 $<sup>^{(</sup>av)}$  stated by the CÆSAR compiler.